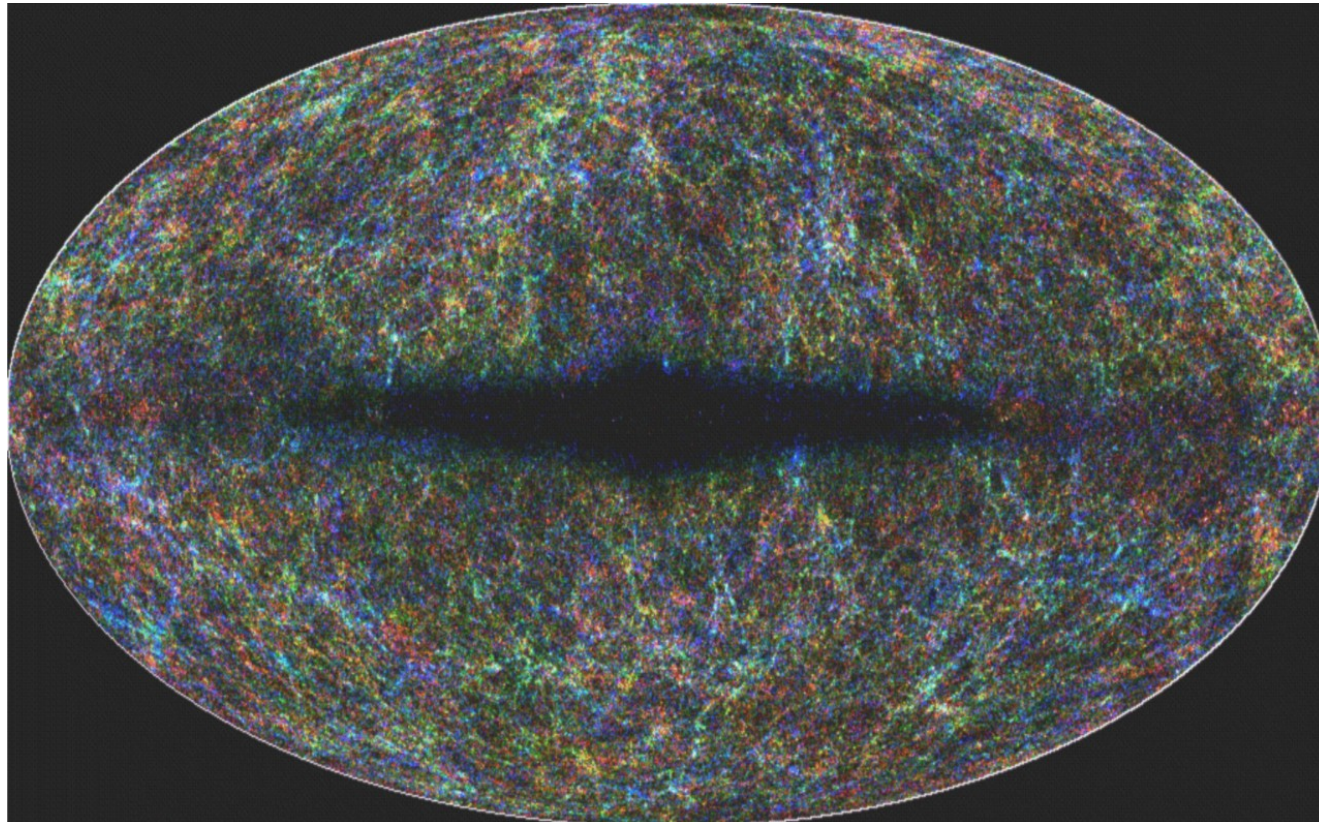


The vacuum, the Higgs field, and modern cosmology

John Peacock



Some big questions in cosmology:

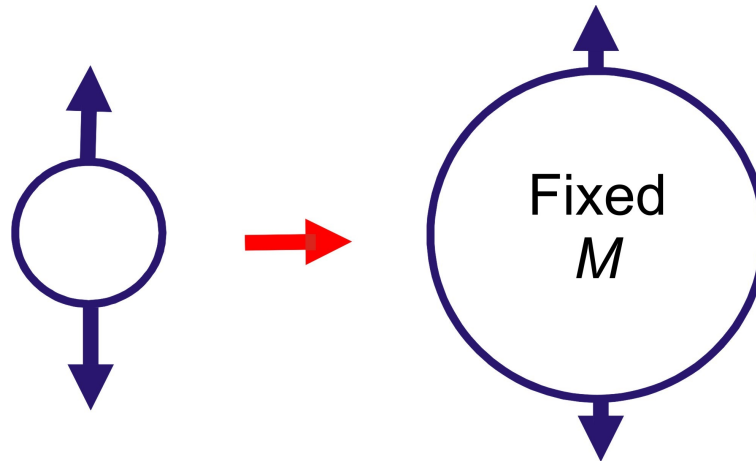
Why is the universe expanding?
What happened before the big bang?

The modern answer: because the vacuum has weight

- **Given different names:
cosmological constant
vacuum energy
dark energy**

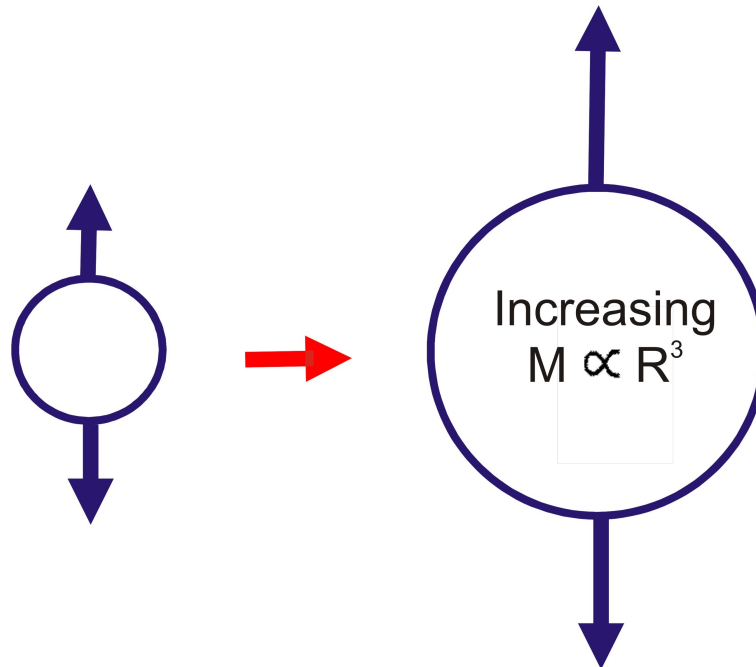
Empty space has antigravity

Ordinary matter:
expansion slows
as it expands,
since gravitational
energy is less



$$V = GM/R$$
$$\propto 1/R$$

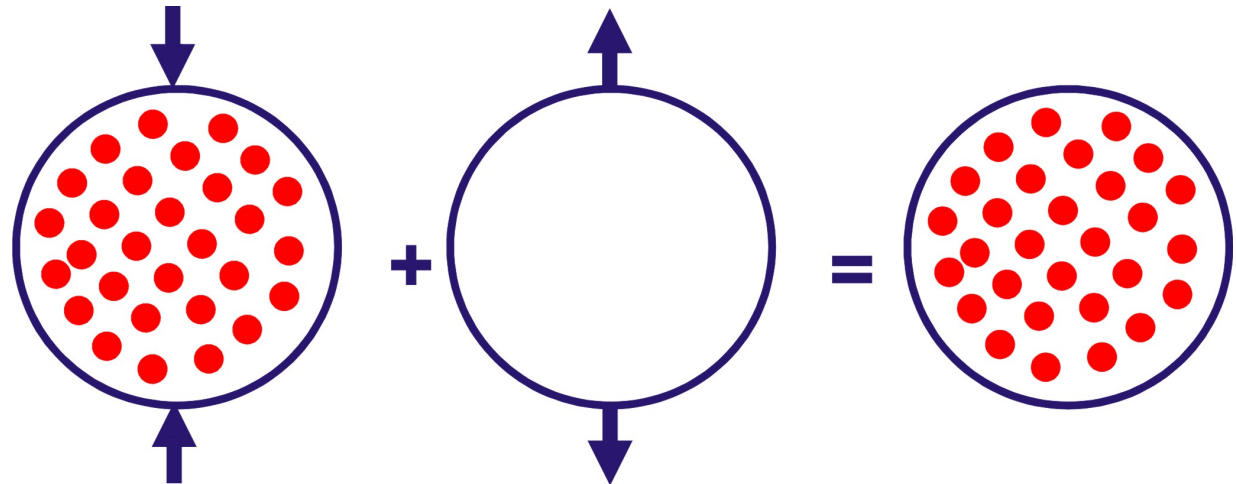
A sphere of
vacuum increases
mass as it
expands, so
gravitational
energy goes up



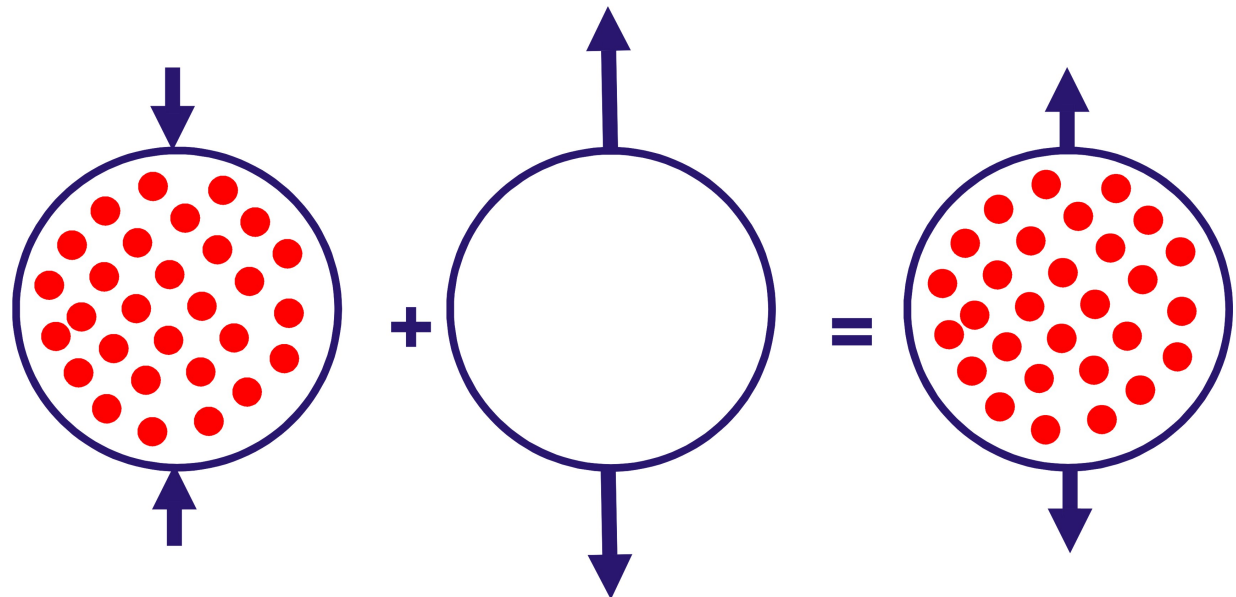
$$V = GM/R$$
$$\propto R^2$$

Vacuum energy: Einstein's missed chance

1917: Einstein's
static universe
balanced gravity and
repulsion from
cosmological constant
- abandoned after
Hubble



Now: 'Dark Energy'
can cause the
expansion of the
universe to accelerate



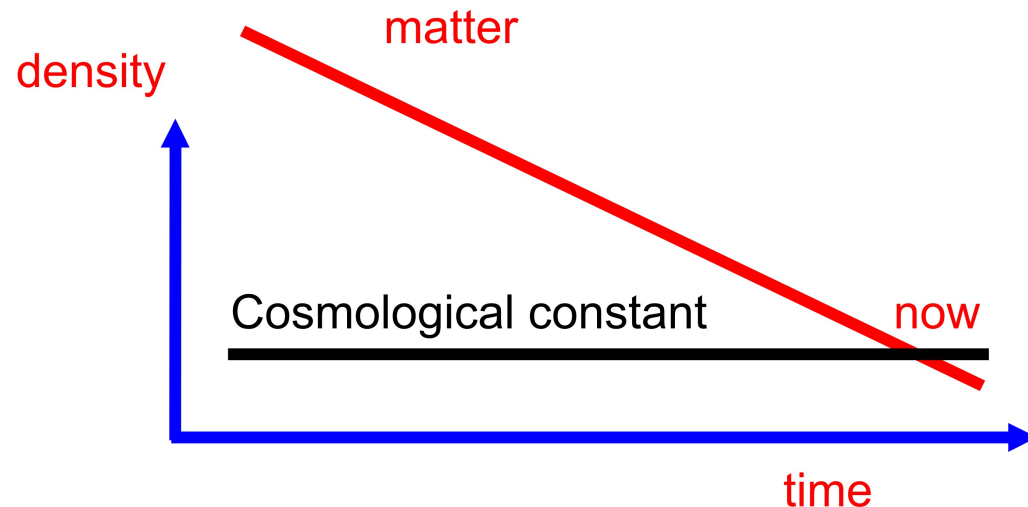
The observed vacuum density

This accelerating expansion is seen in astronomical data (2011 Nobel Prize):

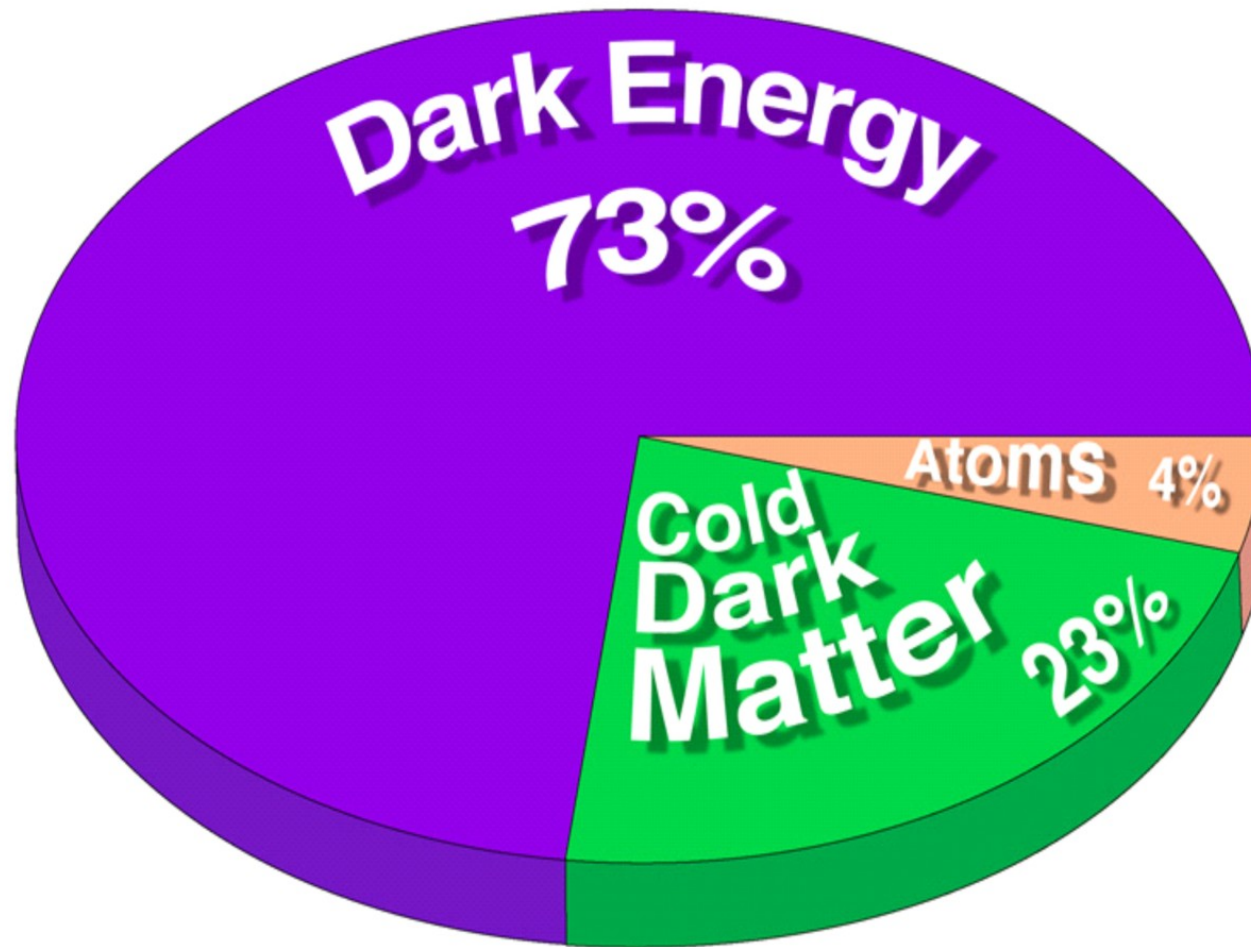
$$\text{Observed vacuum density} = 6 \times 10^{-27} \text{ kg m}^{-3}$$

Acceleration only recent as vacuum density was negligible in the past

The 'why now' problem:

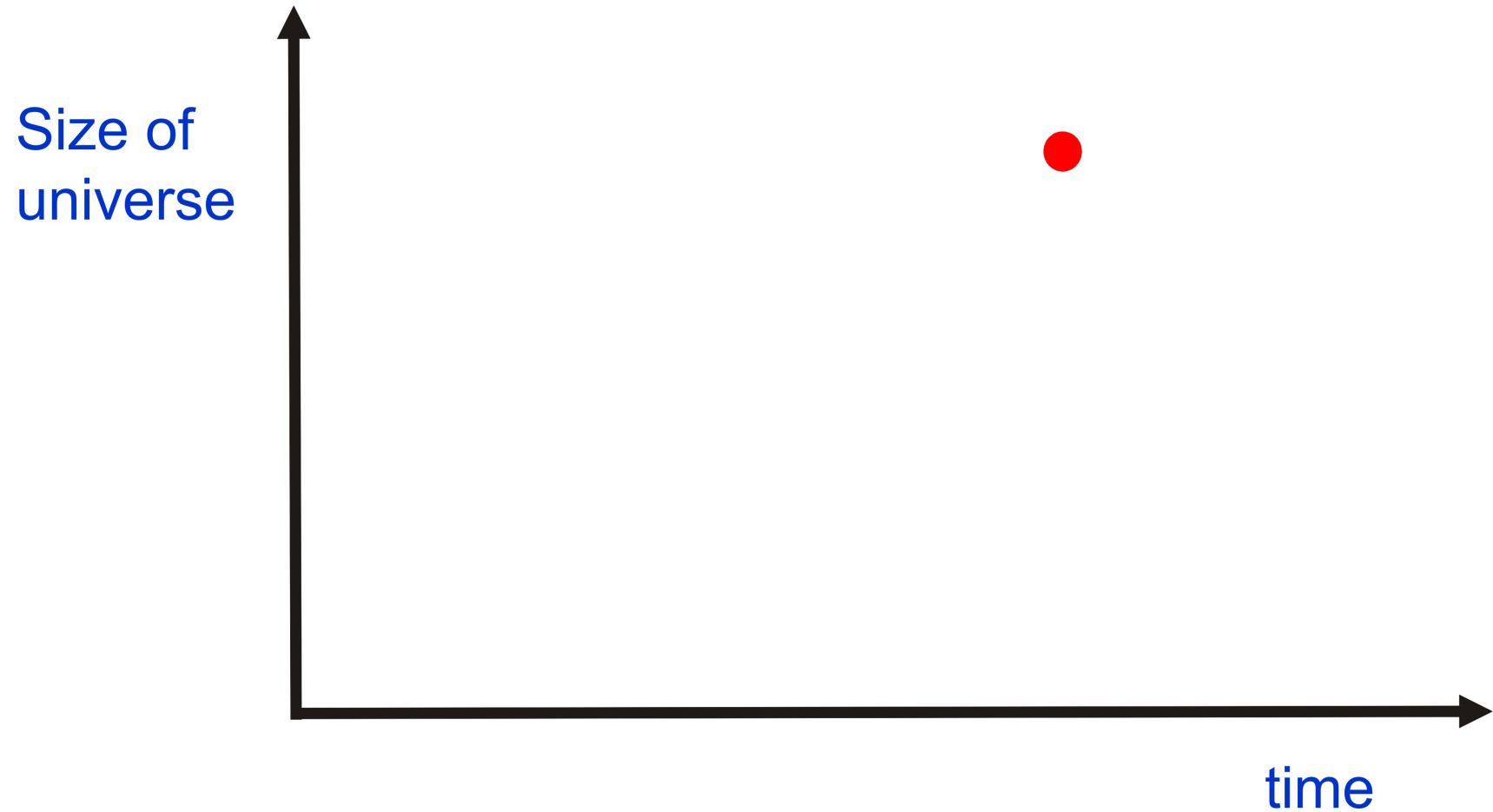


The puzzling universe

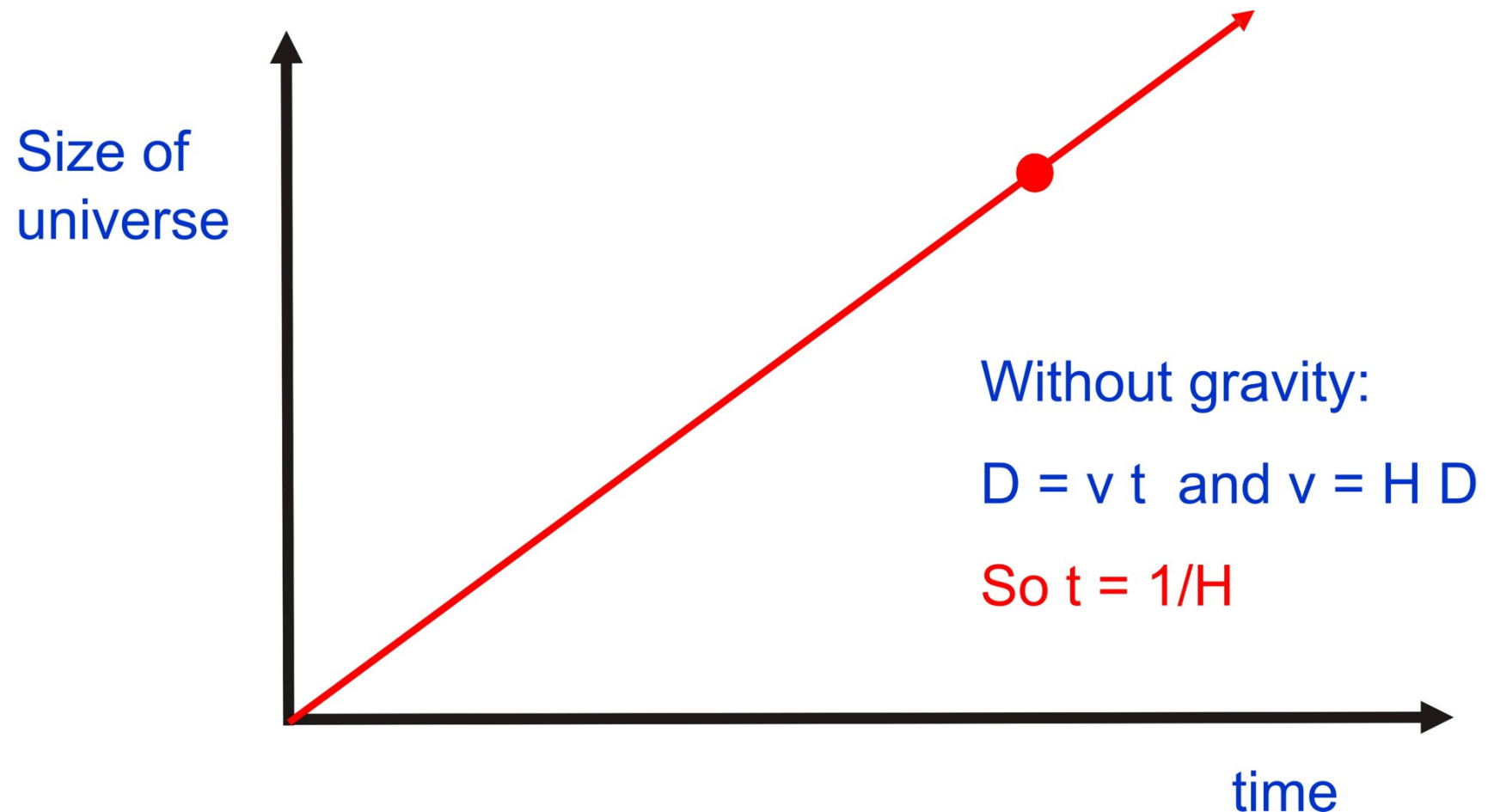


Plus about 0.01% radiation: more important in the past

The Big Bang and cosmic acceleration

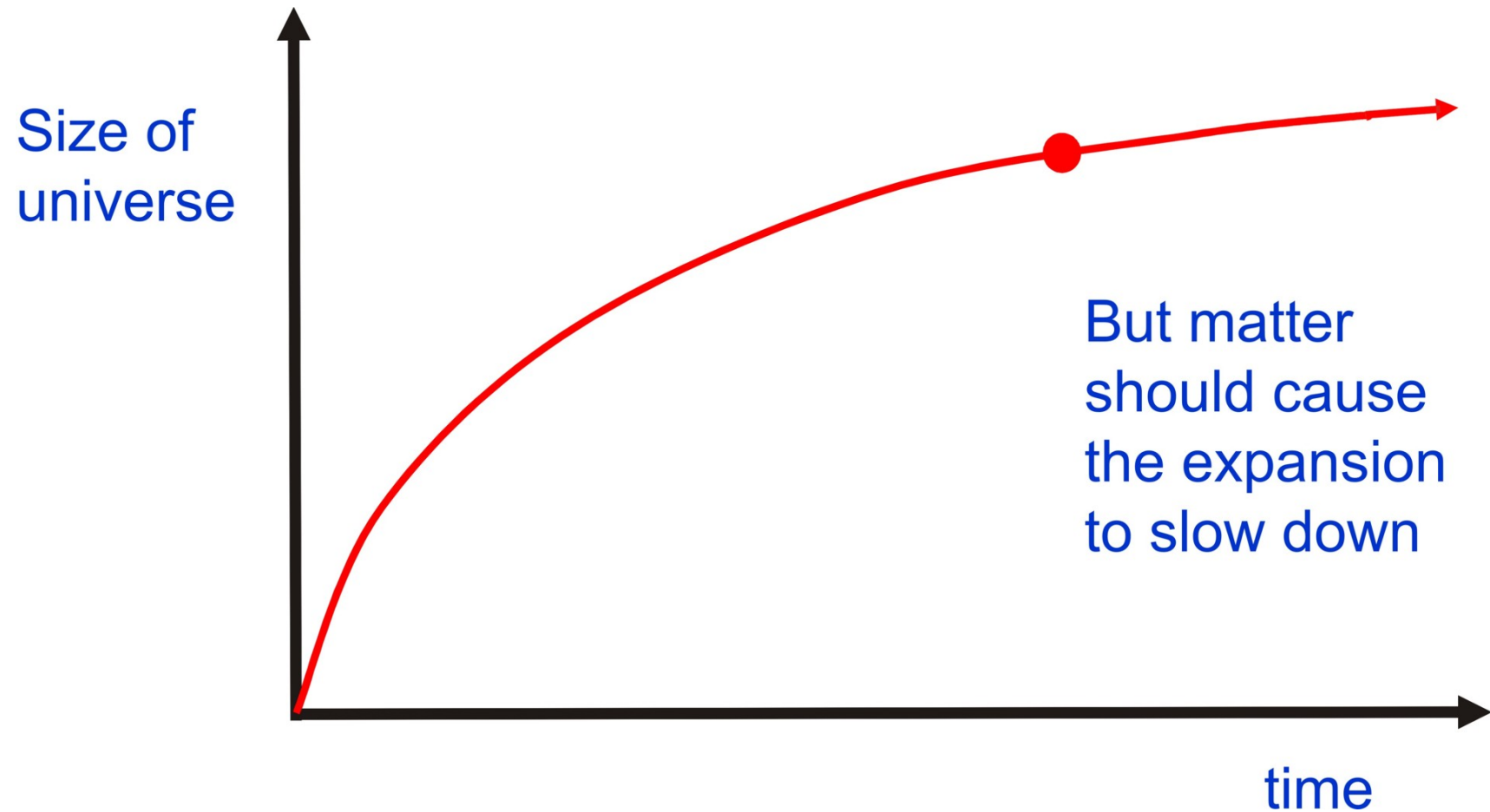


The Big Bang and cosmic acceleration

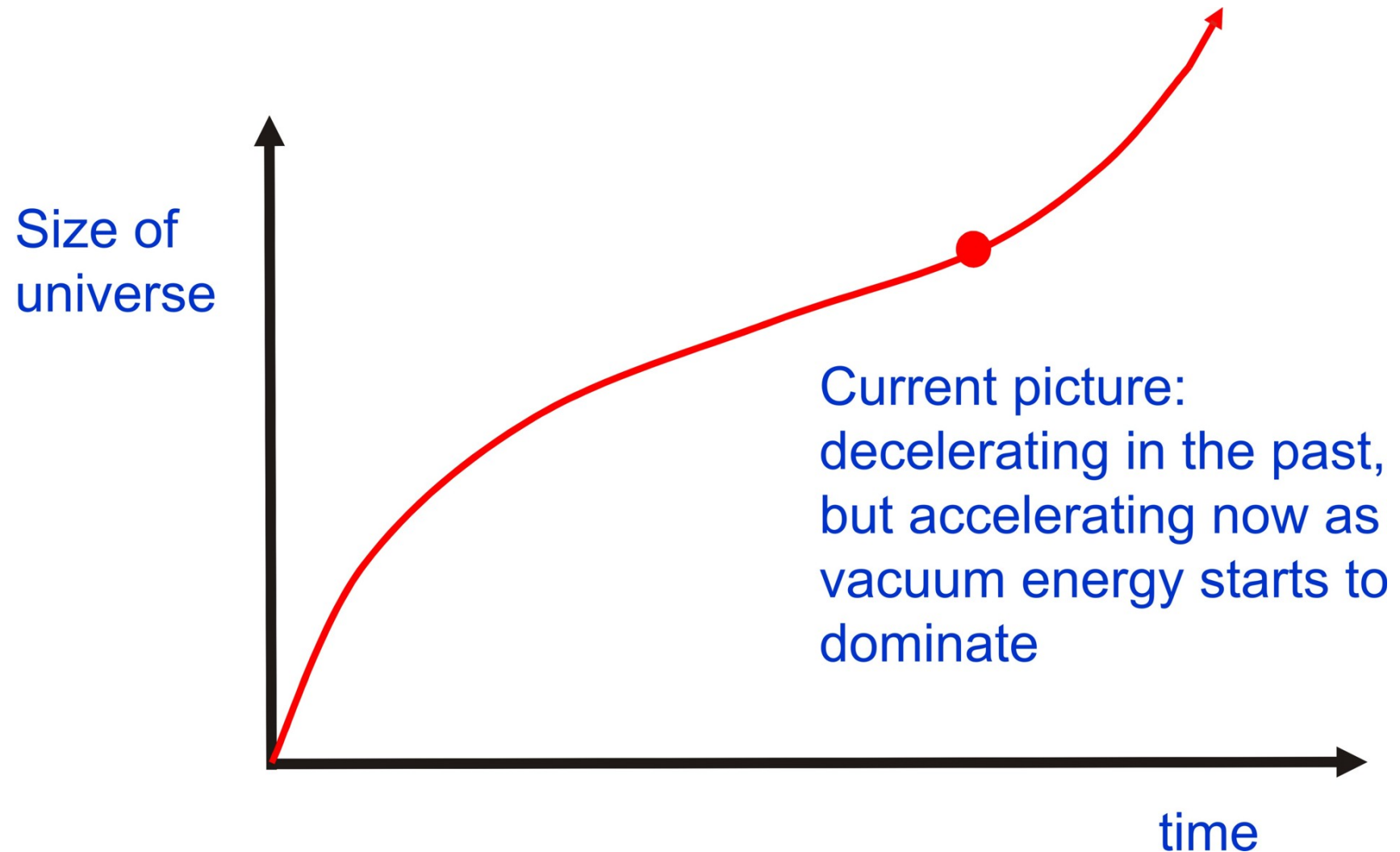


The Big Bang: zero size and infinite density $1/H = 14$ billion years ago

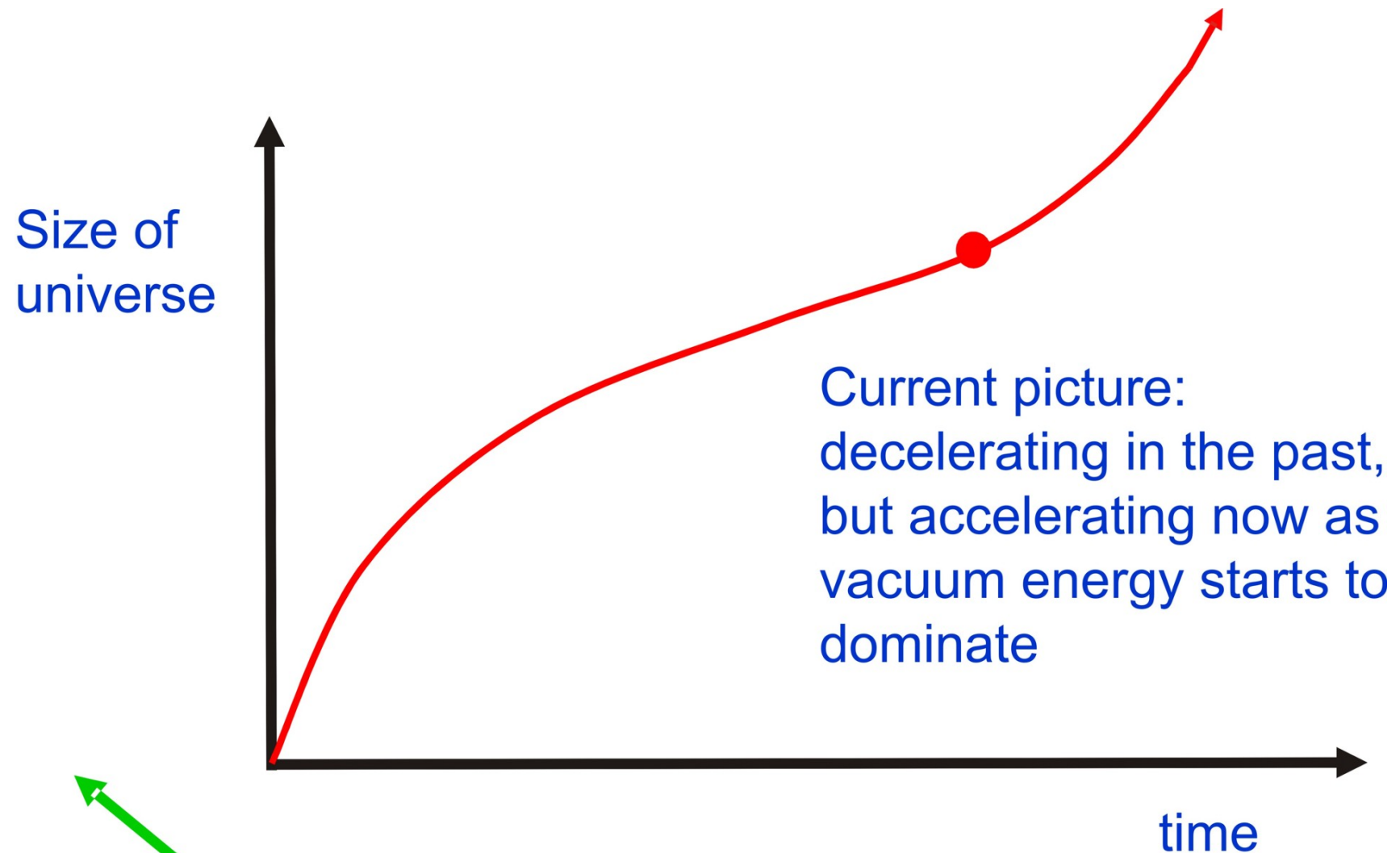
The Big Bang and cosmic acceleration



The Big Bang and cosmic acceleration



The Big Bang and cosmic acceleration



Obvious question: what happened here?

**But how can the vacuum weigh
anything?**

Isn't it empty by definition?

Physics of the subatomic realm:

The uncertainty principle (1927)

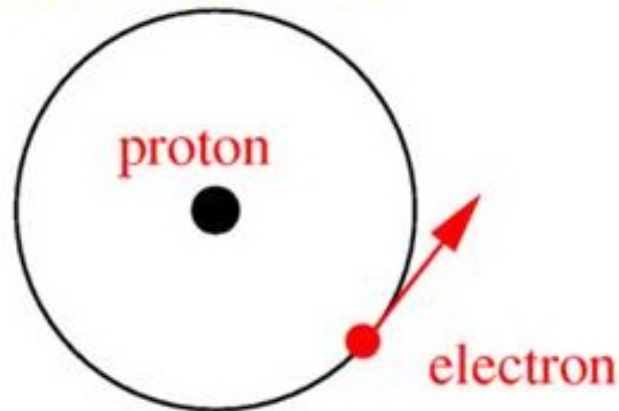
$$\Delta(mv)\Delta(x) \gtrsim \hbar$$

Precise knowledge of both position
and speed is impossible



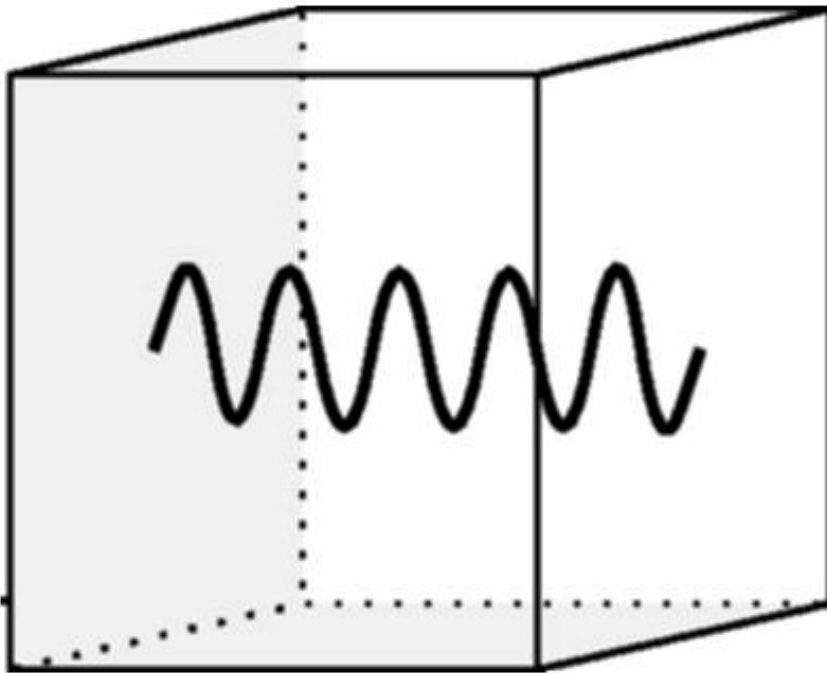
Werner Heisenberg (1901 - 1976)

Sizes of atoms



Uncertainty in speed of electrons
= speed of light
if size of atom = 10^{-12} m

The vacuum of fields: zero-point energy



Energy in
electromagnetic wave
mode of frequency ν
 $= (n + 1/2)h\nu$
n photons and zero-point
energy (inevitable from
uncertainty principle)

- The vacuum is all $n=0$, so some energy remains

The embarrassment of the vacuum density

Need to sum zero-point energy over all photon frequencies -
but then the answer is infinite

Stop at some maximum photon energy (= new physics) and
convert energy density to mass density via $E = Mc^2$

Predicted vacuum density $\sim 10^{36} (E_{\text{max}}/10 \text{ TeV})^4 \text{ kg m}^{-3}$

Observed vacuum density $\sim 10^{-26} \text{ kg m}^{-3}$

So energy scale of new physics is $\sim 0.001 \text{ eV}??$

Need some other contribution to cancel the zero-point energy